## **Theory & Experiment**

#### **Daniel Reta**

www.danielreta.com

DIPC Community Seminar – March 16<sup>th</sup> 23





**Basque Foundation for Science** 



## Outline

- Motivation
- Molecular Magnetism
  - Experimental characterisation
  - Theory and computation
- Single Molecule Magnets
  - > What makes an SMMs and why do we focus on Dy(III)?
  - > Molecular design: from static to dynamic properties
- Organic Radicals
  - > How to trick metal-free molecules into not forming bonds: topology
  - Impact of structural flexibility
- What's next?

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~ 10 minutes

~ 10 minutes

~ 5 minutes

• Quantum information

Grover algorithm in a <sup>159</sup>Tb(III)Pc<sub>2</sub> **qudit** single molecule transistor



Quantum information ٠

> Grover algorithm in a <sup>159</sup>Tb(III)Pc<sub>2</sub> qudit single molecule transistor





#### Improving quantum coherences by operating at clock transitions (CT) in a Lu(II) 5d<sup>1</sup>



Chem. Soc. Rev., 2012, 41, 7464-7478 Phys. Rev. Lett. 2017, 119, 187702 Adv. Mater. 2019, 31, 1806687

• OLEDs

Spin-statistics limit Quantum Efficiency

Conventional fluorescence



Chem. Soc. Rev., 2017, 46, 915-1016





• Synthetic chemistry

Massive substrate scope



High yields and "mild" conditions

By-product: volatile aromatic in place of tin or silicon waste



Science, 2022, 377, 1323–1328



• Experimental characterisation -

• Experimental characterisation – DC magnetometry measures moment varying field and temperature



*Experimental characterisation* – **AC** magnetometry measures moment varying <u>field</u>, <u>temperature</u> and <u>AC frequency</u> •

T (K)



Access to relaxation of magnetisation characteristic time  $(\tau)$ 

 $\chi^{real}$  $\chi^{im}$ 

ω (Hz)

exp

T (K)

τ

т<sup>n</sup>

Ct

**spin-orbit** coupled systems

Experimental characterisation – EPR measures spin transitions varying field and temperature •



• *Experimental characterisation* – electronic structure interrogated with <u>complementary</u> methods



Access to **static** & **dynamic** properties of **spin-only** and **spin-orbit** coupled systems



- A physically meaningful model spin Hamiltonian is formulated for the system
- Data is fitted (global) to validate, refine or discard the model
- Initial guess values are obtained from ab initio methods
- PHI<sup>1</sup> or EasySpin<sup>2</sup> are customarily used

1 J. Comp. Chem., **2013**, 34, 1164–1175 2 J. Magn. Reson. **2006**, 178(1), 42-55



magnetisation characteristic time (au





• Theory and computation –

- Theory and computation Geometry optimisation with Density Functional Theory (DFT)
  - > Both in gas-phase (*Gaussian*) and periodic conditions (*Crystal, VASP, Phonopy*)
  - For <u>spin-only</u> systems:
    - Hybrid, GGA, meta-GGA, range-corrected functionals & standard basis sets
  - ➢ For <u>spin-orbit</u> coupled systems:
    - Exchange-correlation functionals & ECPs diamagnetic analogue with actual isotopic mass for normal modes

- Theory and computation Electronic structure with DFT & multiconfigurational methods (CASSCF, PT2, MRCI)
  - ➢ For <u>spin-only</u> systems:
    - $\Delta E$  between spin-adapted (*OpenMolcas*) states describe model spin Hamiltonian parameters (J, ZFS,  $t/_U$ , …)
    - Mapping approaches to employ broken symmetry solutions (*Gaussian*)
    - Standard basis sets

Exact

Spin-adapted

broken-symmetry

$$\widehat{H}_{elec} = -\sum_{i=1}^{N} \frac{1}{2} \nabla_i^2 - \sum_{i=1}^{N} \sum_{A=1}^{M} \frac{Z_A}{r_{iA}} + \sum_{i=1}^{N} \sum_{j>1}^{N} \frac{1}{r_{ij}}$$

Non-relativistic & time-independent

$$\widehat{H}^{HDVV} = -\sum_{\langle i,j \rangle} J_{ij} \widehat{S}_i \cdot \widehat{S}_j$$
$$|\Psi\rangle_{MC} = \sum_I c_I |\phi_I\rangle$$

$$\widehat{H}^{Ising} = -\sum_{\langle i,j \rangle} J_{ij} \widehat{S}_i^{\ z} \cdot \widehat{S}_j^{\ z}$$

$$|\Psi\rangle_{BS} = |\phi\rangle$$





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  - ➢ For <u>spin-orbit</u> coupled systems (*OpenMolcas*) :
    - Relativistic corrections: scalar 2<sup>nd</sup>-order Douglas-Kroll-Hess and ANO-RCC basis set
    - SOC: AMFI and State-Interaction between appropriate number of states for each spin-multiplicity
    - Parametrisation of ab initio results by means of Crystal Field Theory

$$\widehat{H}_{CF} = \sum_{k=2,4,6} \sum_{q=-k}^{k} B_k^{\ q} \theta_k \widehat{O}_k^{\ q}$$

 $B_k^{q}$ : Crystal Field Parameters (CFPs)  $\theta_k$ : Operator equivalent factors  $\hat{O}_k^{q}$ : Stevens operators (LC of  $\hat{L}_Z$ ,  $\hat{L}_+$ ,  $\hat{L}_-$ )

- Theory and computation Spin dynamics with master matrix & 1<sup>st</sup> order TDPT
  - Description of <u>spin-phonon</u> coupling:
    - Gas-phase molecular normal modes
    - Transition rates are calculated with Fermi's golden rule
    - Orbach process
  - > <u>Dynamics</u>:
    - Master matrix formalism
    - Solution yields how long it takes to reach equilibrium au
    - Solve at different temperatures for direct comparison to experimental relaxation profiles
    - Identify main deactivation pathways and *hope* to affect them with molecular design



• What makes an SMM and why Dy(III)?

Slow relaxation of magnetisation  $\rightarrow$  roughly  $10^5 < \tau(s) < 10^2$  at 2 K,  $\tau(s) < 10^{-4}$  as hot as possible

> Key ingredient is <u>magnetic anisotropy</u>, achieved with large <u>spin-orbit coupling</u> (SOC)

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*Example*: Dy(III)  $4f^9$  electronic configuration. 4f orbitals are shielded by filled atomic shells  $\rightarrow$  unquenched L

 $\frac{5}{2} \le J \le \frac{15}{2}$ 

How are they distributed?

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Axial ligand fields are key

 $\blacktriangleright$  States with largest  $m_I$  are <u>stabilised</u>; states with smallest  $m_I$  are <u>destabilised</u> –  $\Delta E$  informs of  $U^{eff}$ 



**Fig.** Free-ion charge density plots for the  $m_J$  states of the ground Hund's rule term of Dy(III) as derived by Sievers.<sup>1</sup> Figure credit: J. G. C. Kragskow.

1 J. Sievers, Zeitschrift für Physik B, Condensed Matter **1982**, *45*, 289-296.

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 $\succ$   $U^{eff}$  is a key indicator of a SMM performance (static) – <u>How easy it is to relax over the barrier</u>







• Our approach to ab initio spin dynamics

#### Single Molecule Magnets

• Our approach to ab initio spin dynamics

Geometry optimisation & frequency calculation of gas-phase molecule (DFT-PBE)

Vibronic coupling – distort along normal modes, calculate electronic structure (CASSCF) and refer to equilibrium one (CFPs)

> Taylor series for CFPs' dependence on distortion to describe *spin-phonon coupling* Hamiltonian

$$\widehat{H}_{CF} = \sum_{k=2,4,6} \sum_{q=-k}^{k} B_k^{\ q} \theta_k \widehat{O}_k^{\ q}$$

$$B_k^{q}(Q_j, Q'_j, \cdots) = B_k^{q}(Q_{eq}) + \sum_{j=1}^{3N-6} Q_j \left(\frac{\partial B_k^{q}}{\partial Q_j}\right)_{eq}$$

$$\widehat{H}_{SP,j} = \sum_{k=2,4,6} \sum_{q=-k}^{k} B_k^{q}(Q_j) \theta_k \widehat{O}_k^{q} = \sum_{k=2,4,6} \sum_{q=-k}^{k} Q_j \left(\frac{\partial B_k^{q}}{\partial Q_j}\right)_{eq} \theta_k \widehat{O}_k^{q}$$

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Calculate **transition rates**  $\gamma_{if}$  for the Orbach process

$$\gamma_{if} = \frac{2\pi}{\hbar} \sum_{j} \left| \left| f \left| \sum_{k=2,4,6} \sum_{q=-k}^{k} \left( \frac{\partial B_{k}^{q}}{\partial Q_{j}} \right)_{eq} \theta_{k} \hat{O}_{k}^{q} \right| i \right| \right|^{2} \left| \langle n_{j} \pm 1 | Q | n_{j} \rangle \right|^{2} \rho_{j} \left( \Delta E_{fi} \right) \right|^{2}$$

 $\langle f | \hat{H}^{e}_{SP,j} | i \rangle \rightarrow$  Does the vibrational motion affect Dy?

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 $\langle n_j \pm 1 | Q | n_j \rangle \rightarrow$  Is the vibrational mode occupied at transition energy?

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 $\rho_j(\Delta E_{fi}) \rightarrow$  How close in energy are the vibration to the electronic state? (only free parameter in our approach)

Nat. comm. 2017, 8, 14620

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Calculate **transition rates**  $\gamma_{if}$  for the Orbach process

Simulate dynamics as a classical kinetic process master matrix

$$\frac{d}{dt}p_i(t) = \sum_{f \neq i} [\gamma_{if}p_f(t) - \gamma_{fi}p_i(t)]$$



Diagonalise matrix  $\Gamma$  at different T and obtain  $\tau$  to compare directly to relaxation profiles. • Our approach to ab initio spin dynamics – comparison to experiment (JACS. 2021, 143, 15, 5943)



- **FWHM** independent.
- Consistent overestimation of τ
  by a factor of *ca*. 10.
- > Correct ordering of the calculated  $\tau$ .
- Our method can be confidently employed as a <u>predictive</u> tool.

Comparison of experimental (circles) and *ab initio* calculated (lines) relaxation rates for **1**– **6**. Fixed fwhm line widths of 6 (blue), 10 (orange), and 20 cm<sup>-1</sup> (green) are employed. • Our approach to ab initio spin dynamics – can we do better? (JACS. 2021, 143, 15, 5943)



- Distances to ligands.
- Angle between ligands and Dy.
- Charge of ligands.



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• How to trick metal-free molecules into not forming bonds: topological stabilisation of open-shell states

Multiple ways to generate **monoradicals**: captodative, photolysis, redox – *not* discussed here

**Di/polyradicals** through extended  $\pi$ -systems and topological criteria: polycyclic aromatic hydrocarbons (PAHs)

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 $\blacktriangleright$  Lattice classification  $\rightarrow$  odd alternant with non-disjoint non-bonding MOs are target





 $N = n^{starred} - n^{non-starred}$  $N^{even} = 0 / N^{odd} = 2$ 

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How much do NBMOs overlap?

A little for even / A lot for odd

(because orthogonal and degenerate,  $S_{ab} \sim 0$  while  $K_{ab} \neq 0$  with  $\Delta E_{ST} = -2K_{ab}$ )

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Broken bonds to access diamagnetic state? 0 for even / 1 for odd

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Caution: these are approximate guidelines derived for idealised systems. Real molecules are MUCH trickier

- > Other crucial factors for radical stabilisation: kinetic (steric) and thermodynamic (delocalisation)
- Radicals are particularly sensitive to solvent effects
- Nevertheless useful

• Impact of structural flexibility – A molecular junction (Nano Lett. **2016**, *16*, 3, 2066–2071)

Experimental inconsistencies (IETS)



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Computational insight

- > Ising Hamiltonian to calculate exchange interaction as  $\hat{H} = \sum_{\langle i,j \rangle} J_{ij} \hat{S}_i^z \hat{S}_j^z$  with  $J_{12} = J_{23} = J_{13} = J$  (isosceles)
- $\blacktriangleright \text{ Broken symmetry (DFT) approach: } HS = |\alpha\alpha\alpha\rangle, LS = |\alpha\alpha\beta\rangle = |\alpha\beta\alpha\rangle = |\beta\alpha\alpha\rangle \rightarrow E_{|LS\rangle} E_{|HS\rangle} = J$



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Building blocks towards low-dimensionality systems

Previous failed synthetic efforts imposed planarity



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Can the inherent structural flexibility be exploited?



- > B3LYP calculations in periodic & gas-phase to compare structural and magnetic properties of different conformers
- > Broken symmetry approach to 1<sup>st</sup> neighbours interactions

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- > B3LYP calculations in periodic & gas-phase to compare structural and magnetic properties of different conformers
- > Broken symmetry approach to 1<sup>st</sup> neighbours interactions
- > Linear vs helix:

Helix structure is **stabilised** 2.8 Kcal/mol per radical center

J is 18% larger in helix (~ 390 cm<sup>-1</sup>)

> Ferromagnetism & chirality on the same molecular platform



• Impact of structural flexibility – Chirality meets ferromagnetism

Let's speculate

- > Synthetically feasible
- Structural anisotropy induces magnetic anisotropy
- Enantiomeric separation
- ➢ Functional



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Proposal as spin-filter

Transport calculations (?)



#### **Acknowledgements**



The University of Manchester

N. F. Chilton

J. G. C. Kragskow (*Bath*)

G. Gransbury

**UNIVERSITAT** DE BARCELONA

F. Illas

I. De P. R. Moreira

J. M. Bofill



Euskal Herriko Unibertsitatea

J. Ugalde (KT)

L. Lezama

D. Mills

F. Ortu (*Leicester*)

C. Goodwin

P. Evans (*Newcastle*)



